

Solutions to Even problems for Section 1.7 - pg. 54 - 56

8. $(2 + -5)/2 = -3/2$

12. $(13 + -6)/2, (8 + -6)/2 = (7/2, 2/2) = (3.5, 1)$

20. $(1 + x)/2 = 5, (12 + y)/2 = -8$ You know the coordinates of the midpoint, but you are missing the coordinates of one of the endpoints

$1 + x = 10, 12 + y = -16$ Multiply both sides by 2

$x = 9, \quad y = -28 \quad S = (9, -28)$

26. $\sqrt{(12 - -8)^2 + (6 - 18)^2} = \sqrt{(20)^2 + (-12)^2} = \sqrt{400 + 144} = \sqrt{544} = \sqrt{16 * 34} = 4\sqrt{34} = 23.3$

30. $\sqrt{(-3 - 5)^2 + (-4 - 5)^2} = \sqrt{(-8)^2 + (-9)^2} = \sqrt{64 + 81} = \sqrt{145} = 12.0$

34. Everett = $(-3, 5)$ and Fairfield = $(-8, -3)$

$\sqrt{(-3 - -8)^2 + (5 - -3)^2} = \sqrt{(5)^2 + (8)^2} = \sqrt{25 + 64} = \sqrt{89} = 9.4$

40. a. PQ without the segment symbol over the top refers to the length of PQ

$PQ = \sqrt{(-3 - 5)^2 + (-1 - -7)^2} = \sqrt{(-8)^2 + (6)^2} = \sqrt{64 + 36} = \sqrt{100} = 10$

b. Midpoint of $PQ = (-3 + 5)/2, (-1 + -7)/2 = (2/2, -8/2) = (1, -4)$

44. a. PQ without the segment symbol over the top refers to the length of PQ

$PQ = \sqrt{(4 - 3)^2 + (2 - 0)^2} = \sqrt{(1)^2 + (2)^2} = \sqrt{1 + 4} = \sqrt{5} = 2.2$

b. Midpoint of $PQ = (4 + 3)/2, (2 + 0)/2 = (7/2, 2/2) = (3.5, 1)$

48. a. $A = (-9, -6) \quad B = (6, 6)$

$$AB = \sqrt{(-9-6)^2 + (-6-6)^2} = \sqrt{(-15)^2 + (-12)^2} = \sqrt{225+144} = \sqrt{369} = \sqrt{9*41} = 3\sqrt{41} = 19.2$$

b. Midpoint of $AB = (-9+6)/2, (-6+6)/2 = (-3/2, 0/2) = (-1.5, 0)$

54. Cedar = (-3, 1) City Plaza = (0, 0)

$$\sqrt{(-3-0)^2 + (1-0)^2} = \sqrt{(-3)^2 + (1)^2} = \sqrt{9+1} = \sqrt{10} = 3.2 \text{ miles}$$

58. a. If R is midpoint: $(-4+2)/2, (6+4)/2 = (-2/2, 10/2)$ so R is (-1, 5)

If Q is midpoint: $(-4+x)/2 = 2, (6+y)/2 = 4, (-4+x) = 4, (6+y) = 8$ so R is (8, 2)

If P is midpoint: $(2+x)/2 = -4, (4+y)/2 = 6, (2+x) = -8, (4+y) = 12$ so R is (-10, 8)

b. If R = (-1, 5) then $RQ = \sqrt{(2-(-1))^2 + (4-5)^2} = \sqrt{(3)^2 + (-1)^2} = \sqrt{9+1} = \sqrt{10}$

If R = (8, 2) then $RQ = \sqrt{(2-8)^2 + (4-2)^2} = \sqrt{(-6)^2 + (2)^2} = \sqrt{36+4} = \sqrt{40}$

If R = (-10, 8) then $RQ = \sqrt{(2-(-10))^2 + (4-8)^2} = \sqrt{(12)^2 + (-4)^2} = \sqrt{144+16} = \sqrt{160}$

Yes, this will affect the answer to part a. The only way for the distance to be the square root of 160 is for P to be the midpoint, making it so R has to be (-10, 8)

60. The distance formula stays the same, even in 3-D: $d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2 + (z_1 - z_2)^2}$

$$PQ = \sqrt{(2-(-2))^2 + (3-4)^2 + (4-9)^2} = \sqrt{(4)^2 + (-1)^2 + (-5)^2} = \sqrt{16+1+25} = \sqrt{42} = 6.5$$